

In[1]:= (* plna *)

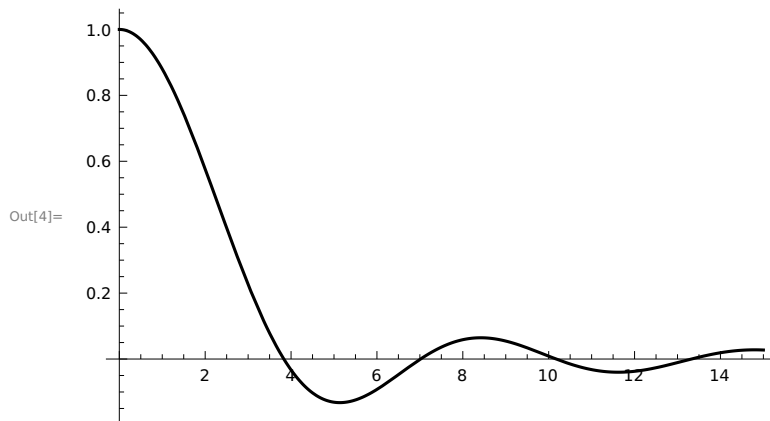
In[2]:= f1 = Integrate[x BesselJ[0, β x], {x, 0, 1}]

Out[2]=
$$\frac{\text{BesselJ}[1, \beta]}{\beta}$$

In[3]:= f1 = f1 / Limit[f1, $\beta \rightarrow 0$]

Out[3]=
$$\frac{2 \text{BesselJ}[1, \beta]}{\beta}$$

In[4]:= p1 = Plot[f1, { β , 0, 15}, PlotStyle \rightarrow Black, PlotRange \rightarrow All]



In[5]:= (* gaussovaska apod - soucet rady *)

In[6]:= Integrate[Exp[-x^2] BesselJ[0, x] x, {x, 0, 1}]

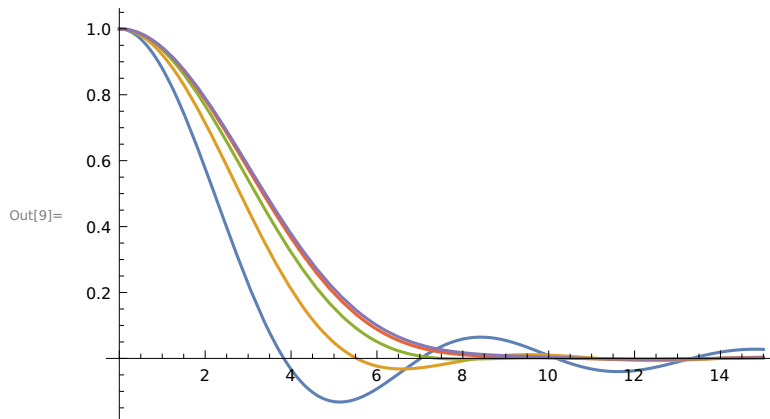
Out[6]=
$$\int_0^1 e^{-x^2} x \text{BesselJ}[0, x] dx$$

In[7]:= $\alpha = 2$;

f2g = Table[Sum[BesselJ[m, β] 2^(m-1) α ^(2m-2) / β^m , {m, 1, n}], {n, 1, 10, 2}];

In[8]:= f2gnorm = f2g / (f2g /. $\beta \rightarrow 0.001$);

In[9]:= Plot[f2gnorm, { β , 0, 15}, PlotRange \rightarrow All]

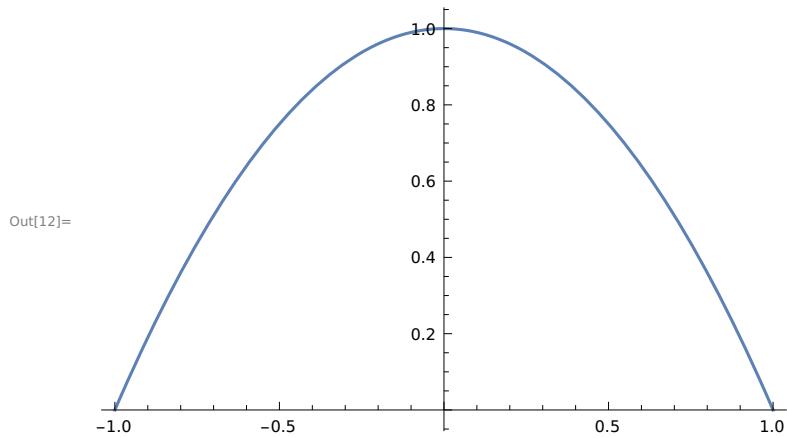


In[10]:= (* kvadraticka apod *)

In[11]:= apod = (1 - x ^ 2)

Out[11]= $1 - x^2$

In[12]:= Plot[apod, {x, -1, 1}]



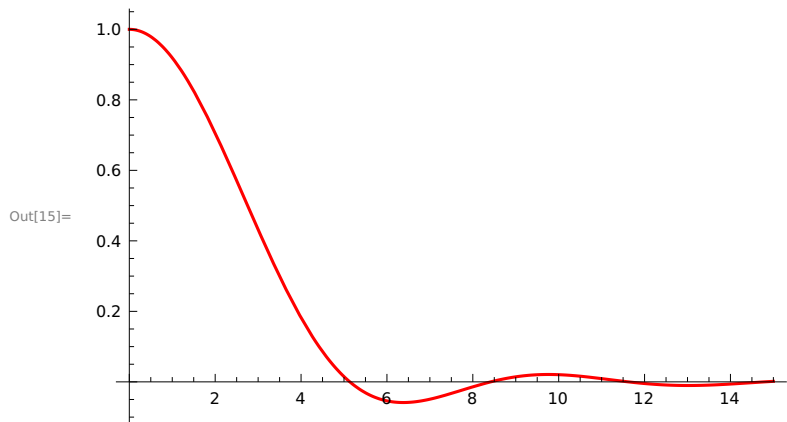
In[13]:= f2 = Integrate[apod x BesselJ[0, β x], {x, 0, 1}]

Out[13]= $\frac{2 \text{BesselJ}[2, \beta]}{\beta^2}$

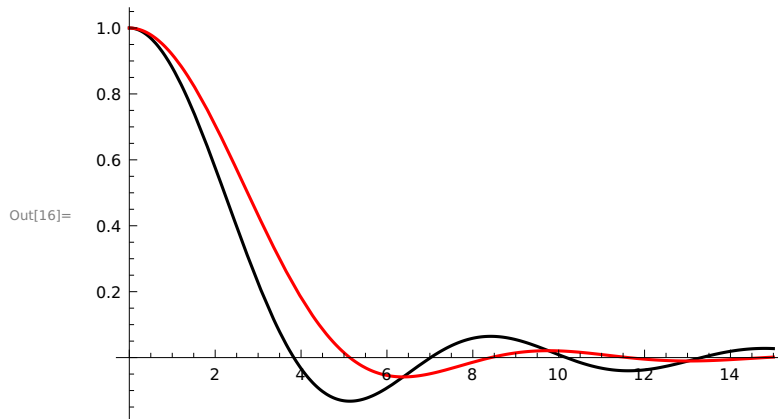
In[14]:= f2 = f2 / Limit[f2, $\beta \rightarrow 0$]

Out[14]= $\frac{8 \text{BesselJ}[2, \beta]}{\beta^2}$

In[15]:= p2 = Plot[f2, { β , 0, 15}, PlotStyle \rightarrow Red, PlotRange \rightarrow All]



In[16]:= Show[{p1, p2}]

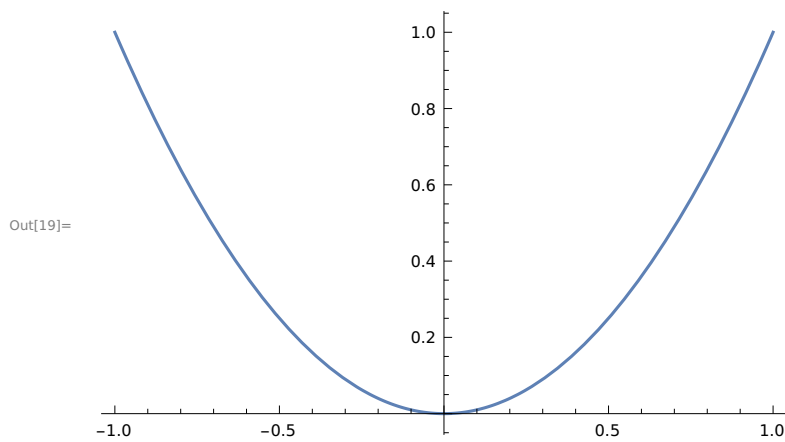


In[17]:= (* kvadraticka inverzni apod *)

In[18]:= invapod = x ^ 2

Out[18]= x^2

In[19]:= Plot[invapod, {x, -1, 1}]



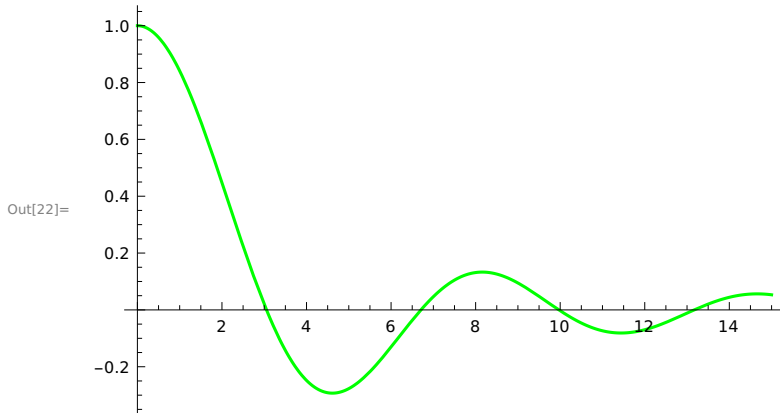
In[20]:= f3 = Integrate[invapod x BesselJ[0, β x], {x, 0, 1}]

Out[20]=
$$\frac{2 \text{BesselJ}[2, \beta] - \beta \text{BesselJ}[3, \beta]}{\beta^2}$$

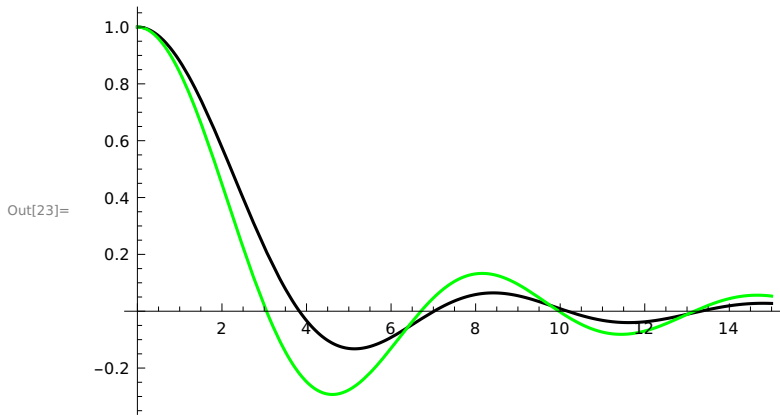
In[21]:= f3 = f3 / Limit[f3, $\beta \rightarrow 0$]

Out[21]=
$$\frac{4 (2 \text{BesselJ}[2, \beta] - \beta \text{BesselJ}[3, \beta])}{\beta^2}$$

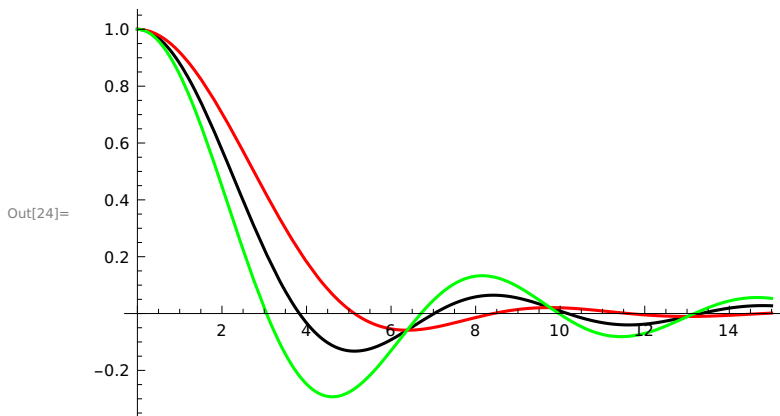
In[22]:= **p3 = Plot[f3, {β, 0, 15}, PlotStyle → Green, PlotRange → All]**



In[23]:= **Show[{p1, p3}]**



In[24]:= **Show[{p1, p2, p3}]**



In[25]:= **(* uzavrena energie *)**

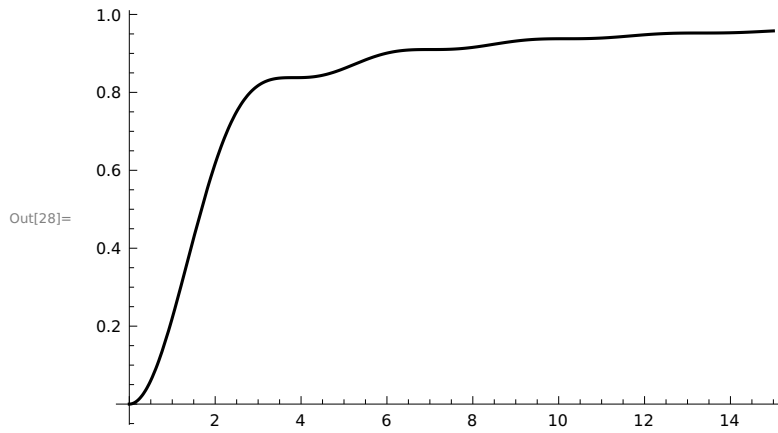
In[26]:= **tot1 = Integrate[β f1 ^ 2, {β, 0, r}, Assumptions → r > 0]**

Out[26]= $-2(-1 + \text{BesselJ}[0, r]^2 + \text{BesselJ}[1, r]^2)$

In[27]:= **tot1 = tot1 / Integrate[β f1^2, { β , 0, Infinity}]**

Out[27]= $1 - \text{BesselJ}[0, r]^2 - \text{BesselJ}[1, r]^2$

In[28]:= **p1b = Plot[tot1, {r, 0, 15}, PlotStyle -> Black, PlotRange -> All]**



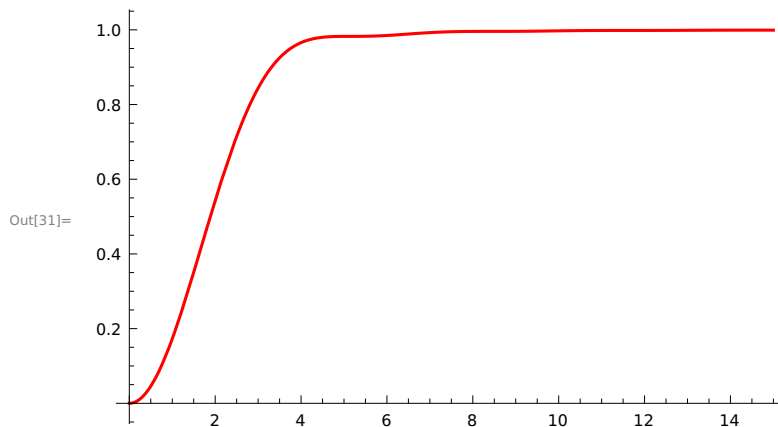
In[29]:= **tot2 = Integrate[β f2^2, { β , 0, r}, Assumptions -> r > 0]**

Out[29]= $\frac{1}{3 r^4} (8 (r^4 - 4 r^2 \text{BesselJ}[0, r]^2 + 16 r \text{BesselJ}[0, r] \text{BesselJ}[1, r] - 4 (4 + r^2) \text{BesselJ}[1, r]^2)$

In[30]:= **tot2 = tot2 / Integrate[β f2^2, { β , 0, Infinity}]**

Out[30]= $\frac{1}{r^4} (r^4 - 4 r^2 \text{BesselJ}[0, r]^2 + 16 r \text{BesselJ}[0, r] \text{BesselJ}[1, r] - 4 (4 + r^2) \text{BesselJ}[1, r]^2)$

In[31]:= **p2b = Plot[tot2, {r, 0, 15}, PlotStyle -> Red, PlotRange -> All]**



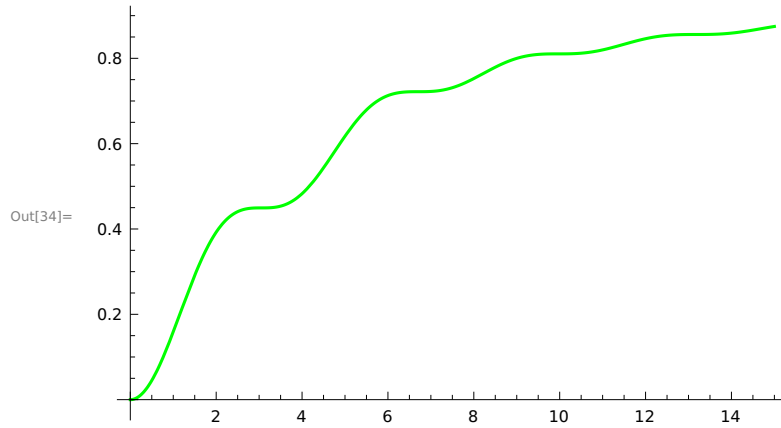
In[32]:= **tot3 = Integrate[β f3^2, { β , 0, r}, Assumptions -> r > 0]**

Out[32]= $-\frac{1}{3 r^4} (8 (-r^4 + r^2 (4 + 3 r^2) \text{BesselJ}[0, r]^2 - 16 r \text{BesselJ}[0, r] \text{BesselJ}[1, r] + (16 - 8 r^2 + 3 r^4) \text{BesselJ}[1, r]^2)$

```
In[33]:= tot3 = tot3 / Integrate[ $\beta$  f3^2, { $\beta$ , 0, Infinity}]
```

$$\text{Out[33]} = -\frac{1}{r^4}(-r^4 + r^2(4 + 3r^2)\text{BesselJ}[0, r]^2 - 16r\text{BesselJ}[0, r]\text{BesselJ}[1, r] + (16 - 8r^2 + 3r^4)\text{BesselJ}[1, r]^2)$$

```
In[34]:= p3b = Plot[tot3, {r, 0, 15}, PlotStyle -> Green, PlotRange -> All]
```



```
In[35]:= Show[{p1b, p2b, p3b}]
```

